Laboratório Interinstitucional de e-Astronomia (LineA)

Constructing a pipeline to constrain cosmology with galaxy clusters

LineA Webinar

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September 15, 2017





Introduction Halo Abundance Formalism Observations of Galaxy Clusters Statistical Methods Observational Effects Simulation Results Science Portal Conclusions

Content

Introduction Pipeline Cosmology Galaxy Clusters

- Halo Abundance Formalism
- Observations of Galaxy Clusters
- Statistical Methods
- **Observational Effects**
- Simulation Results
- Science Portal
- Conclusions



- The study of cosmology has experienced a rapid progress in the last few decades.
- Thanks to surveys such as WMAP (Hinshaw et al., 2013) & PLANCK (Planck Collaboration et al., 2016), the energy content of the Universe at the present epoch has been well characterized as:
 - dark energy (~ 70%)
 - ▶ dark matter (~ 25%)
 - ▶ baryonic matter (~ 5%)
- The modern approach relies on the use of large surveys using statistical quantities.
- Galaxy clusters are the largest structures in the Universe. The abundance is extremely sensitive to expansion and to growth of perturbations.











Einstein Equation

$$G_{\mu\nu} - \Lambda g_{\mu\nu} = 8\pi G T_{\mu\nu}$$

FRW Metric

$$ds^{2} = dt^{2} - a^{2}(t) \left[d\chi^{2} + f^{2}(\chi) d\alpha^{2} \right]$$

Friedmann's equations

$$\begin{array}{rcl} H^2(a) & = & \displaystyle \frac{8\pi G}{3}\bar{\rho}(a) \\ & \displaystyle \frac{\ddot{a}}{a} & = & \displaystyle -\frac{4\pi G}{3}\Big[\bar{\rho}(a)+3\bar{P}(a)\Big] \end{array}$$



Hubble Factor

$$H(z) = H_0 \sqrt{\Omega_{\Lambda} + \Omega_k (1+z)^2 + \Omega_m (1+z)^3 + \Omega_r (1+z)^4}$$







- Dark Matter Halos
- Galaxy Agglomeration
- Several Observational probes (Optical, X-Ray, SZ)



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Halo Abundance Formalism Mass Functions

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Halo Abundance Formalism Halo Mass-function

Fraction of Matter in Halos

$$F(M) = \frac{1}{\sqrt{2\pi}\sigma(M)} \int_{\delta_c}^{\infty} d\delta \exp\left[-\frac{\delta^2}{2\sigma^2(M)}\right] = \frac{1}{2} \operatorname{erfc}\left[\frac{\delta_c^2}{\sqrt{2}\sigma(M)}\right]$$

Press and Schechter (1974)

The differential comoving mean halo number density

$$\frac{d\bar{n}}{d\ln M} = -\frac{\bar{\rho}_m}{M} \frac{dF}{d\ln M} = \frac{\bar{\rho}_m}{M} \frac{d\ln\sigma^{-1}}{d\ln M} \sqrt{\frac{2}{\pi}} \frac{\delta_c}{\sigma} \exp\left[-\frac{\delta_c^2}{2\sigma^2}\right]$$
$$\frac{d\bar{n}(z,M)}{d\ln M} = \frac{\bar{\rho}_m}{M} \frac{d\ln\sigma^{-1}}{d\ln M} f(\sigma)$$

Halo Abundance Formalism

Mass-functions:

- Press and Schechter (1974) (Sphericall)
- Sheth et al. (2001) (Ellipsoidal)
- Jenkins et al. (2001) (Simulation)
- Tinker et al. (2008) (Simulation)







Introduction

Halo Abundance Formalism

Observations of Galaxy Clusters Object Finder Observational Effects

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Observations of Galaxy Clusters

Techniques for Detecting Clusters

- X ray Observations (Evrard et al., 1996; Vikhlinin et al., 2006; Clerc et al., 2016)
- Sunyaev-Zel'dovich Effect (Carlstrom et al., 2002)
- Cluster Lensing (Dietrich and Hartlap, 2010; Marian et al., 2012; Kacprzak et al., 2016; Peel et al., 2017)
- Optical Clusters

Observational Effects

- Mass-Observable Relation (Lima and Hu, 2007)
- Completeness and Purity (Aguena and Lima, 2016)

$$\frac{d\bar{n}}{d\ln X}\left(\Theta_{cl}\right) = \int dV_{\Theta_{h}} \frac{d\bar{n}}{d\ln M}\left(\Theta_{h}\right) W_{[cl,h]}$$

Observations of Galaxy Clusters

- Halo Finders
- Cluster Finders

Approaches of Finders

- Friends of Friends
- Spherical Overdensity

Optical Cluster Finders

- MaxBCG
- Farrens et al. (2011)
- VT3D (Abdalla et al. in dev.)

- ▶ redMaPPer
- ► VT
- ▶ WaZp

Observations of Galaxy Clusters

Photometric Redshifts

$$\mathcal{P}(z^{\mathrm{phot}}) = \int_0^\infty dz \ \mathcal{P}(z) \mathcal{P}(z^{\mathrm{phot}}|z)$$

Mass-Observable Relation

$$rac{dar{n}}{dM^{
m obs}} = \int_0^\infty dM \; rac{dar{n}}{dM} P(M^{
m obs}|M)$$

Selection Function

Completeness c(M, z) and Purity $p(M^{obs}, z^{phot})$

Corrected Prediction

$$\bar{m}_{\alpha,i} \equiv \Delta \Omega \int_{z_i^{\text{phot}}}^{z_{i+1}^{\text{phot}}} dz^{\text{phot}} \int dz \frac{D_A(z)^2}{H(z)} P(z^{\text{phot}}|z)$$
$$\int_{M_{\alpha}^{\text{obs}}}^{M_{\alpha+1}^{\text{obs}}} dM^{\text{obs}} \int \frac{dM}{M} \frac{d\bar{n}}{d\ln M} P(M^{\text{obs}}|M) \frac{c(M,z)}{p(M^{\text{obs}},z^{\text{phot}})}$$



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Statistical Methods Likelihood Fisher Matrix MCMC sampling

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Statistical Methods

Posterior

$$\mathcal{P}(\Theta|\boldsymbol{O}) \propto \mathcal{L}(\boldsymbol{O}|\Theta) \; \Pi(\Theta)$$

Gaussian Likelihood

$$\mathcal{L} = rac{1}{\sqrt{2\pi \det{(m{\mathcal{C}})}}} \exp{\left[\sum_{ij} rac{(N_i - ar{m}_i) \ C_{ij}^{-1} \ (N_j - ar{m}_j)}{2}
ight]}$$

Poissonian Likelihood

$$\mathcal{L} = \sum_{i} \frac{N_i! \bar{m}_i^{N_i}}{\bar{m}_i}$$

Statistical Methods Likelihood - Fixing Parameter





Statistical Methods Likelihood - Marginalizing over Parameters





Statistical Methods Fisher Matrix

- Assumes Gaussian distribution of the parameters
- Produces Forecasts
- Much Faster $\mathcal{O}(N_{pars})$ than sampling techniques $\mathcal{O}(10^4)$

$$F_{\alpha\beta} = -\left\langle \frac{\partial^2 \ln \mathcal{L}(\mathbf{\Theta})}{\partial \Theta_{\alpha} \partial \Theta_{\beta}} \right\rangle$$

Likelihoods

$$F_{\alpha\beta} = \bar{\boldsymbol{m}}_{,\alpha} \boldsymbol{S}^{-1} \bar{\boldsymbol{m}}_{,\beta}{}^{T} + \frac{1}{2} \operatorname{Tr} \left[\boldsymbol{S}^{-1} \boldsymbol{S}_{,\alpha} \boldsymbol{S}^{-1} \boldsymbol{S}_{,\beta} \right]$$
$$F_{\alpha\beta} = \bar{\boldsymbol{m}}_{,\alpha} \boldsymbol{M}^{-1} \bar{\boldsymbol{m}}_{,\beta}{}^{T}$$
$$F_{\alpha\beta} = \bar{\boldsymbol{m}}_{,\alpha} \boldsymbol{C}^{-1} \bar{\boldsymbol{m}}_{,\beta}{}^{T} + \frac{1}{2} \operatorname{Tr} \left[\boldsymbol{C}^{-1} \boldsymbol{S}_{,\alpha} \boldsymbol{C}^{-1} \boldsymbol{S}_{,\beta} \right]$$

Statistical Methods

- Monte Carlo Markov Chain
- Sampling from probability distributions
- Much Faster $\mathcal{O}(10^4)$ than grid $\mathcal{O}(20^{N_{pars}})$
- Does not assume Gaussianity as FM

1. From a point Θ in parameter space, propose a random step Θ_s

- (a) If $\mathcal{P}(\Theta_s) > \mathcal{P}(\Theta)$: take the step $(\Theta \to \Theta_s)$
- (b) Else: Génerate a random number $R \in [0:1]$
 - i. If the ratio $\mathcal{P}(\Theta_s)/\mathcal{P}(\Theta) > R$: take the step $(\Theta \to \Theta_s)$
 - ii. Else: Remain at the original point Θ
- 2. Repeat step 1 until the distribution of the parameters converge
- Usual formulation is not parallelizable
- Parallel implementation: emcee (Foreman-Mackey et al., 2013)





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- Optical Effects on Cluster Dark Energy Constraints
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How is the cluster cosmology affected by the optical effects?

Aguena and Lima (2016)

Survey

- ► flat wCDM with Planck 2015 cosmology $(h^2 \Omega_m, h^2 \Omega_b, w, A_s, n_s, \Omega_{DE})$
- priors of 1% on $(h^2\Omega_m, h^2\Omega_b, A_s, n_s)$
- ▶ area of 5000 deg², covariance within 500 cells of 10 deg²
- ▶ 0.1 ≤ z ≤ 1.0
- ▶ 7 Mass bins: $M_{th}^{\text{obs}} = 10^{13.8} M_{\odot}/h$, $\Delta \log[M^{\text{obs}}/(M_{\odot}h^{-1})] = 0.2$
- Mass-Observable distribution Gaussian in log space:

$$P(M^{\rm obs}|M) = \frac{1}{\sqrt{2\pi\sigma_{\ln M^{\rm obs}}^2(M)}} \exp\left[\frac{\left(\ln M^{\rm obs} - \ln M - \ln M_{bias}^{\rm obs}(M)\right)^2}{2\sigma_{\ln M^{\rm obs}}^2(M)}\right]$$

Mass-Observable

$$\ln M_{bias}^{\rm obs}(z) = A_b + n_b \ln(1+z)$$

$$\frac{\sigma_{\ln M^{\rm obs}}^2(z,M)}{0.2^2} = 1 + B_0 + B_z(1+z) + B_M\left(\frac{\ln M_s}{\ln M}\right)$$

 $^{*}M_{s} = 10^{14.2}M_{\odot}/h$

Completeness and Purity

$$egin{array}{rcl} c(M,z) &=& rac{[M/M_c(z)]^{n_c}}{[M/M_c(z)]^{n_c}+1}, \ p(M^{
m obs},z) &=& rac{[M^{
m obs}/M_p^{
m obs}(z)]^{n_p}}{[M^{
m obs}/M_p^{
m obs}(z)]^{n_p}+1} \end{array}$$

Possibilities of Completeness and Purity

case (1):
$$n_c = 3$$
, $n_p = 1$
case (2): $n_c = 1$, $n_p = 3$

case (0):
$$c(M) = 1$$
 , $p(M^{obs}) = 1$





Finding Bias Limit

Bias inside the constraint:

$$b(\Theta_{\alpha}) \leq \gamma \left(F^{-1}\right)_{\alpha\alpha}^{1/2}$$

where $\gamma = 1, 2, 3$ indicate biased predictions inside the 68, 95, 99% confidence levels.





Improvements by including CP and Lowering M_{th}









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Halo Cosmology



Simulation Results BCC Dark Matter Halos

Simulation Specifications

- Aardvark v1.0 catalogs of the Blind Cosmology Challenge (BCC) DES
- ► DM simulation (~ 10,313 deg², 0 < z < 2)</p>
- DM halos (Behroozi et al., 2013, 2012) and galaxies
- Complete above $\sim 4.5 \times 10^{13} M_{\odot} h^{-1}$ ($\sim 5 \times 10^{12} M_{\odot} h^{-1}$)
- \blacktriangleright \sim 30 million halos

Theoretical Prediction Comparison

- 5 mass bins
- 20 redshift bins
- Survey was sub-divided into:
 - 12 pixels (859 deg²)
 - 48 pixels (214 deg²)
 - 768 pixels (13 deg²)
 - 49152 pixels (0.21 deg²)





Testing Theoretical Abundance Prediction





Testing Theoretical Abundance Prediction



Testing Theoretical Covariance Prediction



Simulation Results BCC Dark Matter Halos

Constraining Cosmology

- DM Halos
- $M_{th} = 10^{13.8} M_{\odot} h^{-1}$ (5 bins)
- ▶ 0 < z < 2 (20 bins)</p>
- Tinker MF
- 214 deg²
- $(h, n_s, \Omega_b) =$ (0.72, 0.96, 0.042)





Simulation Results BCC Dark Matter Halos

Best fit

- DM Halos
- $M_{th} = 10^{13.8} M_{\odot} h^{-1}$ (5 bins)
- ▶ 0 < z < 2 (20 bins)</p>
- Tinker MF
- 214 deg²



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Cluster Cosmology



WaZp clusters in BCC

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WaZp

- ▶ Wavelet z Photometric (WaZp) cluster finder (Dietrich et al., 2014)
- z^{phot} slices with overlaps
- Density in each slice is computed via wavelet transformation
- Cylinders across slices are constructed



WaZp clusters in BCC

- ▶ Reduced Area (~ 220 deg²), 0.1 < z < 1.0</p>
- 45,677 Halos with $M > 10^{13} M_{\odot} h^{-1}$
- ▶ 39,861 Clusters with *N* > 3



Proximity Match

Requirements:

$$\begin{cases} |z_{halo} - z_{cluster}| & \leq \sigma_z (1 + z) * \\ \Delta \theta & \leq N \theta_R \end{cases}$$

* Ilbert et al. (2006); Mazure et al. (2007); Arnouts et al. (2007); Ilbert et al. (2009)



WaZp clusters in BCC

Angular Residuals

$$\Delta heta \leq N heta_R = 2N rcsin \left(rac{R}{2D(z_m)}
ight)$$

Mass/Richness Bins





WaZp clusters in BCC

Angular Residuals

$$\Delta heta \leq N heta_R = 2N rcsin \left(rac{R}{2D(z_m)}
ight)$$

Redshift Bins





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Simulation Results WaZp clusters in BCC

Completeness and Purity - Regions in the Sky



Completeness

- No significant directional effects
- Small edge effects

Purity



WaZp clusters in BCC





WaZp clusters in BCC

Redshift Relation



- Scatter is very small
- Test showed including P(z^{obs}|z) had insignificant effect
- P(z^{obs}|z) will not be considered

WaZp clusters in BCC

Mass Richness Relation

$$\log\left[\frac{M^{\rm obs}(M^{\rm cl},z)}{M_{\odot}h^{-1}}\right] = A(z) \log\left[M^{\rm cl}\right] + B(z)$$





WaZp clusters in BCC



$$\sigma_{\ln M^{cl}}(M,z) = \frac{\sigma_0(z)}{1 + \left(\frac{M}{M_{\sigma}(z)}\right)^{n_{\sigma}(z)}}$$



$$\sigma_0(z) = \sigma_{00} + \sigma_{01}(1+z)
\log M_{\sigma}(z) = \log M_{\sigma0} + \log M_{\sigma1}(1+z)
n_{\sigma}(z) = n_{\sigma0} + n_{\sigma1}(1+z)$$



WaZp clusters in BCC

Theoretical Prediction

$$\begin{split} \bar{m}_{\alpha,i} &\equiv \Delta \Omega \int_{z_i}^{z_{i+1}} dz \frac{D_A(z)^2}{H(z)} \int_{M_\alpha^{\rm obs}}^{M_{\alpha+1}^{\rm obs}} dM^{\rm obs} \\ &\int \frac{dM}{M} \frac{d\bar{n}}{d\ln M} P(M^{\rm obs}|M) \frac{c(M,z)}{p(M^{\rm obs},z^{\rm phot})} \end{split}$$

. .



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Theoretical Prediction



Theoretical Prediction



WaZp clusters in BCC

Theoretical Prediction







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- There are many additional issues for galaxy cluster detection
- Collaboration from researchers of different institutes/locations



Pipelines



🕗 Dashboard My Workspace	Pipelines To	ols Data S	erver	Documentation	Help	
	Data Installatio	n	•			
	Data Preparatio	in .	۰E			
DES Science Portal: Wo	Science-Ready	Catalogs	۰ŀ.			
The Science Portal has two instances:	Science Analys	is	•			
Workflows: hosts workflows for Data Server, provide access to	Parameter Esti	mation	• •	reation of Value-Adde	ed Catalog	s (VACs) and for Science Analysis.
The system is designed to be self-evid	Utilities		• 0	Catalog Comparison		
The Science Portal is a facility develop	Special Sample	15		Diuster-Cluster Matchi	ing	the helpdesk@linea.opv.br
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Product Log - Matching

	Utilities Cluster-Cluster Mai Process ID: 1874	tching		
Process Summary Results Comments				
Summary Properties Completeness and Puri	ty Centering and Redshift Most Massive Matches			
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Matching	Component Version			V02 19 00
External Footprints	Matching Code Version			2.10.0
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	Index Label	[1]		[2]
	Total Number of Objects Used	81805		85955
	Match (including Multiple)	48557		
	Two Way Match	45194		45194
	Specific Matching Types		Galaxy Clusters 3	Galaxy Clusters 18
	Match (Galaxy Clusters 18 -> Galaxy Clusters 3)		46090	46090
	Match (Galaxy Clusters 18 -> Galaxy Clusters 3)(Including Multi	ple)	52905	48050
	Match (Galaxy Clusters 3 -> Galaxy Clusters 18)		46024	46024
	Match (Galaxy Clusters 3 -> Galaxy Clusters 18)(Including Multi	ple)	52063	47992
-	t	Footprints		
	Footprint Info	Galaxy Cluster	rs 3	Galaxy Clusters 18
	Original Number of Objects in Each Catalog	140899		232400
	Objects Cropped by limits	26484		128977
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	Objects Cropped by Galaxy Clusters 3 Footprint	14		17468
	Footprint NSIDE	512 (~ 6.9 arcmin) - External Used	[4096 (~ 51.5 arcsec)]	512 (~ 6.9 arcmin)
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Product Log - Matching

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Dashboard

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Install Catalogs	2016-03-08 15:40:13	01:51:56	1	•	RED LSS Sample	2017-06-09 15:59:29	00:06:55	2	•
Install Mangle Mask	2016-06-10 10:21:14	05:49:15	1	•	Catalog Association				
Install Bright Mask	2016-06-10 10:15:36	00:01:07	2	•					
Install Depth Maps	2016-09-20 15:46:18	01:09:07	2	•					
Systematic Maps	2016-06-13 12:47:35	12:43:31	2	•					
Zeropoint Correction	2017-01-18 15:47:17	05:48:03	Z	•					
Coarse Depth Map				•	Science Workflows				
		Total: 29:36:44			Pipeline	Start	Duration	Runs	Stat
					ACF GE				
Asta Preparation					ACF LSS	2017-06-09 11:39:57	02:12:36	1	•
Pipeline	Start	Duration	Runs	Status	StarHorse	2017-05-12 16:12:48	30:05:20	1	•
SG Separation	2017-07-06 10:41:39	02:37:33	2	•	WAZP	2017-09-04 15:18:46	00:39:30	4	•
Spectroscopic Sample	2017-09-14 10:35:29	00:00:26	20						
Training Set Maker	2017-09-14 10:50.47	00:17:25	ш	•					
Photo-z Training	2017-07-12 15:33:23	01:30:13	17	•					
Photo-z Compute	2017-07-28 18:43:13	03:28:14	21	•	Parameter stimation				
Galaxy Properties				•					
		Total: 7.53.51			Utilities				
Science-ready Catalogs					Pipeline	Start	Duration	Runs	State
Pipeline	Start	Duration	Runs	Status	Catalog Comparison	2016-08-05 14:04:35	01:08:43	- P	•
Cluster	2017-09-11 10:27:48	05:04:02	18	•	Cluster-Cluster Matching	2017-06-15 00:27:34	06:00:45	24	•
GE					Cluster-Halo Matching	2017-04-18 09:20:56	00:14:51	1	•
GA	2017-05-12 13:37:02	01:35:01	3		Concatenate Fields	2017-02-01 23:33:59	00:51:11	4	•
LSS	2017-06-07 16:14:24	02:42:36	2		Download Tool	2017-09-13 13:02:01	00:00:35	30	•
Georgie					Export Table	2017-06-29 15:03:40	38:34:42	209	•

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Conclusions



- Galaxy clusters comprise a powerful tool for constraining cosmology.
- It is extremely important to consider the observational effects.
- The proposed functional form for the corrections on the prediction agrees with simulation measurements at medium and high richnesses.
- ► The pipeline for halos was shown to be operating properly.
- ► The pipeline for clusters will be operating soon.
- We (DES-Brazil) are producing a WaZp catalog for the DES Y1 data in the portal.

Thank You!

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